Speed Control of Photovoltaic Pumping System

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Abstract- In this paper, an intelligent speed controller of permanent magnet synchronous motor is investigated. The motor speed leads a photovoltaic water pumping system. The photovoltaic generator is connected to chopper converter that is controlled by technical fuzzy logic with a view to operate at the maximum power point whatever the temperature and solar irradiance variation. Thus, to analyze the performance of speed control between the proportional integrator controller and fuzzy logic controlled. A synthesis of these speed controllers is developed and the simulations with Matlab/Simulink according to the progressive and abrupt load tests are shown and discussed.

Keywords Photovoltaic, water pumping, fuzzy logic controller, MPPT, simulation.

1. Introduction

Due to the ever increasing demand in power, several laboratories have oriented their research design and the development of structures for the production of electrical energy [1-3].

In particular, the geographical location of the Algeria that is strategic with the average solar daily amount on the horizontal plane is in order of 5 to 7 kWh/m²/day and an average daily sun is of the order of 7 to 9 hours [4]. However, the decision maker’s aim through the encouragement of the production of electrical energy based solar energy in order to solve the problem of managing energy for isolated areas.

The PV system has the disadvantage of a low efficiency, low performances and a very high cost. Furthermore, the photovoltaic generator (PVG) is non-linear, including its operation or the maximum power (MPP) which depend of irradiation, temperature and a variation of a load [5, 6].

Therefore, monitoring of the maximum power point tracking (MPPT) used as a strategy to control DC - DC converter online to track the maximum output power point for PVG to various climatic conditions of operation. The reference of DC voltage is obtained by the MPPT algorithm [7]. There are many methods for calculating the MPPT [8-12]. Among which is the most used is the perturbation and observation method, other techniques have been developed equally offered, in order, with the hope of minimizing the number of devices or enhance performance of generating the control signal Pulse Width Modulation (PWM) of DC-DC converters.

In this work, we consider the study of a photovoltaic pumping system. This system plays the role of an essential means to need water for remotes areas. Although it accepts big quantities of solar radiation throughout the year, so PV water pumping system (PVWPS) is perfectly solution of water in sahara sites [13].

There is provided this system for controlling the speed of a permanent magnet motor synchronous (PMSM) which is supplied a centrifugal pump. The PMSM is primarily used because of their relatively low cost and robustness [14]. Where, this motor was supplied by power AC converter. The role of the fuzzy observer is designed to optimize the overall performance of the system, leading accordingly to maximize the speed and flow of water from the centrifugal pump coupled with the speed of rotation and modular variable number of work steps to obtain the highest system performance for all conditions [15].

The continuation of this article is made up of the following sections: Section II discusses the modelling system topologies of photovoltaic water pumping systems and...
features. Section III deals the space vector pulse modulation. Section IV discusses the MPPT based on fuzzy logic. Section IV discusses the speed control of PMSM based on fuzzy logic controller (FLC) and compare with traditional PI regulator. Finally, Section V presents the simulation and results obtained with the proposed techniques.

2. Modelling of System

The structure of photovoltaic water pumping considered in this work is illustrated by “Fig. 1”.

![Fig. 1. Synoptic bloc of photovoltaic water pumping](image)

2.1. Photovoltaic Generator

A cell photovoltaic is component the most elementary of a module PV [16], the current generated by these cells is very weak. A solar module is a combination amongst solar cells, a module PV [16], the current generated by these cells is very weak. A solar module is a combination amongst solar cells, which are joined in series and parallel. The main electrical equation of PV module is illustrated by “Fig. 2”.

![Fig. 2. Equivalent circuit for the photovoltaic model](image)

The main electrical equation of PV module is illustrated by “Eq. (1)” [17, 18]:

\[
I_L = I_{ph} - I_D - I_{sh} \quad (1)
\]

\[
I_L = N_p I_{ph} - N_p 1 \left\{ \exp \left[ \frac{q(U_{pv}+I_{ph}R_s)}{akT} \right] - 1 \right\} - \frac{U_{pv}+I_{ph}R_s}{R_{sh}} \quad (2)
\]

Where,

- \( I_L \): output load current;
- \( U_{pv} \): output voltage of PV array;
- \( I_{ph} \): photocurrent of cell solar;
- \( R_{sh}, R_s \): shunt and series resistance, respectively;
- \( q \): electron quantity’s = 1.60217646 x 10^{-19}C;
- \( k \): boltzmann’s constant, \( k = 1.3806503 \times 10^{-23} \text{J/K} \);
- \( a \): ideal factor of the PV characteristic \( 1 < a < 1.5 \);
- \( I_0 \): current of saturation reverse cell is gived by following Equation:

\[
I_0 = I_{or} \left( \frac{T}{T_i} \right)^3 \exp \left\{ \frac{qE_G}{ka} \left[ \frac{1}{T} - \frac{1}{T_i} \right] \right\}
\]

With,

\[
I_{or} = \frac{I_{scn}}{e^{(\frac{qV_{ocn}}{kT})} - 1}
\]

Where,

- \( T, T_i \): real and reference temperature, respectively;
- \( I_{or} \): saturation reverses current;
- \( E_G \): energy band gap of semiconductor;
- \( V_{ocn} \): nominal open-circuit voltage of the PV module.

Indeed, the relation of photocurrent \( I_{ph} \) is represented by the following relation:

\[
I_{ph} = (I_{sec} + k_c(T - 298)) \frac{G}{1000}
\]

Where,

- \( I_{sc} \): short-circuit current;
- \( G \): solar radiation;
- \( k_c \): coefficient of short-circuit current temperature.

The previous equations show that the climatic conditions radiation solar \( G \) and temperature \( T \) have a considerable impact on the amplitude of the voltage and current of PVG. “Fig. 3” and “Fig. 4” show the variation of power and current depending on the voltage for solar radiation between 200 W/m² to 1000 W/m² at constant temperature \( T=25^\circ C \) and the deferent temperature for -5°C to 55°C with constant solar radiation\( G=1000 \text{ W/m}^2 \), respectively.

![Fig. 3. Power and current characteristics for different solar radiation](image)
Space Vector Pulse Width Modulation (SVPWM) [21]. The AC motor is composed of three independent arms, each arm possesses two semiconductors controlled by the Space Vector Pulse Width Modulation (SVPWM) [21]. The stator voltages of PMSM \( (V_{sa}, V_{sb}, V_{sc}) \) and the photovoltaic current \( (I_{pv}) \) with \( S_a, S_b \) and \( S_c \) are the pulses generator for semiconductors which are exposed respectively as following:

\[
\begin{aligned}
V_{sa} &= \frac{u_{pv}}{3} \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} \cdot S_a \\
V_{sb} &= \frac{u_{pv}}{3} \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} \cdot S_b \\
V_{sc} &= \frac{u_{pv}}{3} \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} \cdot S_c
\end{aligned}
\]

(7)

\[I_{pv} = S_1 + S_b + S_c + I_c\]

(8)

Where, \( i_a, i_b \) and \( i_c \) are the PMSM stator currents and \( I_c = c \frac{du_{pv}}{dt} \) is the MPPT controller required the optimum duty cycle of the semiconductor, who depends of atmospheric conditions, is shown in “Fig. 5”.

2.4. Permanent Magnet Synchronous Motor Model

PMIS model in alpha-beta axis reference can be described by the following mathematical equations:

\[
\begin{aligned}
u_a &= R_s i_a + L_s \frac{di_a}{dt} - \omega_s \Psi_f \sin \theta \\
u_b &= R_s i_b + L_s \frac{di_b}{dt} - \omega_s \Psi_f \cos \theta \\
\Psi_f &= \int (u_a - R_s i_a) \, dt \\
\Psi_f &= \int (u_b - R_s i_b) \, dt \\
T_e &= \frac{3}{2} N_p (\Psi_a i_b - \Psi_b i_a)
\end{aligned}
\]

(9)

(10)

(11)

Where,

\( u_{a,b} \): stator voltage component of PMSM; \\
\( i_{a,b} \): stator current components of PMSM; \\
\( R_s, L_s \): the stator resistance and the inductance, respectively; \\
\( \psi_f \): flux of permanent magnet; \\
\( \omega, \theta \): rotor speed and position, respectively.

2.5. Centrifugal Pump Model

The square of the centrifugal pump torque is proportional to the motor rotation speed motor. Centrifugal pump is the most commonly employed type of pumps, it's capable of pumping the water with high volumes due to its efficiency and its top relatively [22, 23]. The performances \((Q, H \) and \( P)\) are given in terms of the speed using the following relationships:

\[
\begin{aligned}
Q' &= Q Z \\
H' &= H Z^2 \\
P' &= P Z^3
\end{aligned}
\]

(12)

With \( Z = \omega' / \omega \).

Where,

\( \omega', \omega \): speed and nominal speed, respectively; \\
\( Q', H \) : water flow and the nominal water flow, respectively; \\
\( H', H \) : height and total height, respectively; \\
\( P', P \) : power and nominal power, respectively.

3. Space Vector Pulse Width Modulation

The SVPWM technique of reducing torque ripples, current and keep a form of circular flow. Therefore, the
SVPWM control delivers a modulator separated for each of the three phases, and then the vector of control overall approximated over a period gives reference voltages. Firstly, SVPWM is made to generate impulses at switches inverter that powers the PMSM motor using the effective voltage vector.

This technique is much in demand in the field of the control, it’s effect on ripple current and torque are remarkable, which is why it is the most used by researchers and industry, it is used to determine the sequence of ignitions and extinctions components of the converter and thus to minimize the harmonics and obtain optimum performance of the applied machine voltages. SVPWM technique is different from that at PWM place to employ a separate each phase modulator for each phase, the reference voltages are given by a vector approximated overall control over modulation. Especially since the recent technological advances in field of digital computers (DSP, microprocessors and microcontrollers), made his industrial location pretty simple.

The structure of two levels of three phase inverter allows generate eight (08) the vectors voltages which are presented according “Fig. 6”. Particularly, two vectors (V0=000 and V7=111) are zero, this to defined the six sectors.

![Volages space vector diagram for the two-level inverter](image)

**Fig. 6.** Volages space vector diagram for the two-level inverter

### 3.1. Judgment of Sector Number

The judgement of sector is defined according to the following variables:

\[
\begin{align*}
U_{rfa} &= U_{\beta} \\
U_{rfa} &= U_{\alpha \sqrt{3}} - U_{\beta} \\
U_{rfa} &= -U_{\alpha \sqrt{3}} - U_{\beta}
\end{align*}
\]

*(Equation (13))* gives the section number (N) [23]. The “Table 1” shows the corresponding relation between N and sector:

<table>
<thead>
<tr>
<th>Sector number</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>3</td>
<td>1</td>
<td>5</td>
<td>4</td>
<td>6</td>
<td>2</td>
</tr>
</tbody>
</table>

### 3.2. Calculation of Switch Time

From the vectors for different sectors, table 2 shows the execution time of each switch of the inverter.

<table>
<thead>
<tr>
<th>Sector number</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>T1</td>
<td>-Z</td>
<td>Y</td>
<td>X</td>
<td>Z</td>
<td>-Y</td>
<td>-X</td>
</tr>
<tr>
<td>T2</td>
<td>X</td>
<td>Z</td>
<td>-Y</td>
<td>-X</td>
<td>-Z</td>
<td>Y</td>
</tr>
</tbody>
</table>

With,

\[
\begin{align*}
X &= U_{\beta} T \sqrt{3} / U_{dc} \\
Y &= (3U_{a} + U_{\beta \sqrt{3}}) T / 2U_{dc} \\
Z &= (-3U_{a} + U_{\beta \sqrt{3}}) T / 2U_{dc}
\end{align*}
\]

*(Equation (15))*

### 3.3. Definition Time Value of Voltage Vector

The vector voltage time is given according to the following sector:

\[
S_a = (T - T_1 - T_2) / 4 \\
S_b = 0.5T_1 + S_a \\
S_c = 0.5T_2 + S_b
\]

*(Equation (16))* Assign T1cs, T2cs and T3cs according to “Table 3”, where the action time of three phase are defined and compared with triangular wave, finally we obtained deferent time of SVPWM.

<table>
<thead>
<tr>
<th>Sector number</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>T1cs</td>
<td>S_b</td>
<td>S_a</td>
<td>S_a</td>
<td>S_c</td>
<td>S_c</td>
<td>S_b</td>
</tr>
<tr>
<td>T2cs</td>
<td>S_a</td>
<td>S_b</td>
<td>S_b</td>
<td>S_a</td>
<td>S_a</td>
<td>S_b</td>
</tr>
<tr>
<td>T3cs</td>
<td>S_c</td>
<td>S_b</td>
<td>S_c</td>
<td>S_a</td>
<td>S_b</td>
<td>S_a</td>
</tr>
</tbody>
</table>

### 4. Fuzzy Logic for MPPT Controller

The controller which is based on fuzzy logic is called artificial intelligence, it’s becoming increasingly popular where used for tracking the MPPT. It is possess the advantage of this technique is that it can operate with low precision values of input and does not require modelling of the system and processes the linear and nonlinear operation. The principle of fuzzy logic is based on two input variables: the error and the derivative of the error, it is also based on an output variable which is called the duty cycle; it is the trigger converter to wait for the maximum power point that waits it is determined by a rule table. In the blurred literature, it involves three steps: fuzzification, inference and defuzzification. The “Fig. 7” presents the diagram of fuzzy logic.

![Structure of fuzzy logic controller](image)

**Fig. 7.** Structure of fuzzy logic controller
The input parameters are associated with the following equations [24]:

\[
\begin{align*}
\Delta e(k) &= e(k) - e(k-1) \\
\Delta v(k) &= v(k) - v(k-1)
\end{align*}
\]

(17)

Where,

\[ P_{pv}(k): \text{instantaneous power of PVG}, \quad V_{pv}(k): \text{instantaneous voltage of PVG}. \]

The fuzzy logic tracks the MPP using the rule of “If A and B, Then C” [24, 25] and the inference calculates the output of the fuzzy logic. Those several methods for inference among the best methods known is Mamdani. And other types for example: compositional rule of inference (CRI), Generalized Modus Ponens (GMP) and Sugeno inference method. In our work the defuzzification applied the center of gravity method to specific the optimum value of duty cycle (d) of FLC [24, 26]:

\[
d = \frac{\sum_{i=1}^{5} \mu(D_i) \cdot d_i}{\sum_{i=1}^{5} \mu(D_i)}
\]

(18)

In the fuzzification stage, variable digital inputs are converted into linguistic variable in our case with the seven values NB: Negative big; NM: Negative medium; NS: Negative small; Z: Zero; PS: Positive small; PM: Positive medium; PB: Positive big, as seen in “Fig. 8”.

**Fig. 8.** Rules of fuzzy logic controller

**Fig. 9.** Surface of fuzzy logic controller

The inference rules will be illustrated in “Table 4” with two input variables as (e) and (\(\Delta e\)) where (d) as the output.

<table>
<thead>
<tr>
<th>(\Delta e)</th>
<th>e</th>
<th>NB</th>
<th>NM</th>
<th>NS</th>
<th>Z</th>
<th>PS</th>
<th>PM</th>
<th>PB</th>
</tr>
</thead>
<tbody>
<tr>
<td>NB</td>
<td>NB</td>
<td>NM</td>
<td>NM</td>
<td>NS</td>
<td>Z</td>
<td>NS</td>
<td>NS</td>
<td>Z</td>
</tr>
<tr>
<td>NM</td>
<td>NM</td>
<td>NM</td>
<td>NS</td>
<td>NS</td>
<td>Z</td>
<td>NS</td>
<td>NS</td>
<td>PM</td>
</tr>
<tr>
<td>NS</td>
<td>NS</td>
<td>NS</td>
<td>NS</td>
<td>Z</td>
<td>PS</td>
<td>PS</td>
<td>PM</td>
<td>PM</td>
</tr>
<tr>
<td>Z</td>
<td>Z</td>
<td>NS</td>
<td>NS</td>
<td>PS</td>
<td>PS</td>
<td>PS</td>
<td>PM</td>
<td>PM</td>
</tr>
<tr>
<td>PS</td>
<td>PS</td>
<td>Z</td>
<td>NS</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
</tr>
<tr>
<td>PM</td>
<td>PM</td>
<td>Z</td>
<td>PS</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
</tr>
<tr>
<td>PB</td>
<td>PB</td>
<td>Z</td>
<td>PS</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
<td>PM</td>
</tr>
</tbody>
</table>

5. Speed Controller

As shown in equation (12), the beginning of photovoltaic pumping water according to the speed rotation of the PMSM motor which drives the centrifugal pump, then we must add a speed controller returns to the start of water constant.

In our work we conceded two types of controllers: a classic controller is the proportional integral (PI) and fuzzy logic (FLC).

5.1. Proportional Integral Regulator

The traditional regulator PI is the most used in regulation because it is simple and reliable in operation. So in our case we used the PI for speed control of PMSM, so the rotor speed \(\omega_r\) and compared with the reference speed \(\omega_{ref}\). As shown in the following equations [27]:

\[
\begin{align*}
\Delta e(x) &= \omega_r(x) - \omega_{ref}(x - 1) \\
\Delta e\Delta x &= e(x) - e(x - 1)
\end{align*}
\]

(19)

The quadrature current reference is given by:

\[
l_{q,ref}(x) = l_{q,ref}(x - 1) + K_{p}\Delta e(x) + K_{i}e(x)
\]

(20)

Where,

- \(e(x)\): speed error of working interval,
- \(e(x-1)\): speed error of previous interval,
- \(K_{i}\) and \(K_{p}\): proportional and integrator speed controller gains, respectively.
5.2. Fuzzy Logic Controller

The fuzzy controller is an intelligent controller defines the laws of control of all the system from adopting rules, he composed two inputs: error and variation in the error rate as expressed in equation (21):

\[
\begin{align*}
    \text{error}(x) &= \omega_r(x) - \omega_r(x-1) \\
    \text{variation in error}(x) &= \text{error}(x) - \text{error}(x-1)
\end{align*}
\] (21)

The “Fig. 10” presents the speed control system then we concede in our paper.

6. Speed Controller

The simulation results of the PV water pumping system are presented. “Fig. 11” presents the simulation diagram of considered system.

“Fig. 12” indicates the evolution of the output voltage, power and current of the photovoltaic generator. We note that the fuzzy controller gives better efficiency in response time of about 0.04s and exceeded acceptable.
Fig. 13. Response of current, electromagnetic and flux controlled by FLC

Depending on the nature of the variation of the load, both tests are introduced. Abruptly changes the mechanical torque ($T_m$) of 1N.m to 3.5N.m at time 0.1s to 0.15s, and progressive change of $T_m$ between 0.25s and 0.3s.

The “Fig. 13” and “Fig. 14” show the test results of control for photovoltaic pumping speed based on FLC and compared with PI corrector. These results show that the fuzzy control ensures the best performances and the oscillations decrease during the starting and the change of the load. Regarding the “Fig. 15” we can see any disturbance of the speed during the progressive load variation.

Fig. 14. Response of currents, electromagnetic and flux controlled by PI

7. Conclusion

The objective of this paper is to study the tracking current and voltage of solar array for to get the optimum point power maximum possible of the PVG. In other, to get regardless of the different climatic conditions such as solar radiation and temperature.

The artificial intelligence controllers can give more performance than traditional controllers for non-linear systems order, since it's most fast, stable and more flexibility was obtained.

The presented method the water quantity regulation based for PMSM which is supplied by photovoltaic system. The speed is controlled by fuzzy controller.

The comparison of the tests results indicates the acceptability of fuzzy logic controller efficiencies. On balance, it made dynamic conditions state. Indeed, there was a greater speed, a good rejection of load disturbance.
Appendix

Table 5. System Parameters

<table>
<thead>
<tr>
<th>PVG Parameters</th>
<th>Ppv = 84,62 (Wc)</th>
<th>Upv = 17,2 (v)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Ipv= 4,85(A)</td>
<td>Ns=15 and Np=1</td>
</tr>
<tr>
<td>PMSM parameters</td>
<td>Rs=2.875(Ω)</td>
<td>Ls=Lr=0.175 (H)</td>
</tr>
<tr>
<td></td>
<td>J=0.08 (Kg.m²)</td>
<td>N=1470 (tr/min)</td>
</tr>
<tr>
<td></td>
<td>Centrifugal pump parameters</td>
<td>Q = 2 (l/s)</td>
</tr>
</tbody>
</table>

References


